Large Arcs in Small Planes

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An arc of degree d in a projective plane is a set of n points with no more than d of them collinear. It is denoted as (n, d)-arc. Examples arise from algebraic curves of degree d. An important task is to determine for each value of d and q the largest value of n for which an (n, d)-arc exists. We are interested in studying large arcs of degree d in PG(2, 11) for small q. A related problem is that of classifying arcs up to projective equivalence. The talk will survey some of the techniques which are used to classify arcs: complete searches with classification using poset classification; liftings of smaller arcs using techniques of Cook, Ball and others; isomorph classification using canonical forms; parallel computing. Iterestingly, largest arcs do not always arise from curves of degree d, so it is of interest to build models for the known examples. Such models may lead to new constructions of arcs and perhaps to infinite families. We will consider specific problems from the plane PG(2, 11), with a particular emphasis on arcs of degree 5.

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