Suborbital Graphs of the Congruence Subgroup $\Gamma^0(N)$

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In this paper, for any positive integer N, we determine the edge conditions of suborbital graphs for the congruence subgroup $\Gamma^0(N)$, $G_{p,q}$, and the suborbital graph of the block $[\infty]$, $F_{p,q}$, which is a subgraph of $G_{p,q}$. Then we give the necessary and sufficient conditions for graphs to contain a triangle, which eventually leads to the conditions for it to be a forest.

Keywords: suborbital graph, congruence subgroup, forest