Irregular Domination in Graphs

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A set S of vertices in a graph G (without isolated vertices) is a total dominating set if for every vertex v of G, there exists a vertex u in S such that the distance d(u, v) between u and v is 1. A set S of vertices of G is an irregular dominating set if the vertices of S can be assigned distinct positive integer labels such that for every vertex v of G, there exists a vertex u in S in such a way that d(u, v) is the label assigned to u. Some results and problems dealing with irregular dominating sets are presented. In particular, the problem of determining the possible structures of irregular dominating sets within a graph is discussed.

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