Geodesic Leech Graphs

Seena Varghese, Federal Institute of Science and Technology, Kerala, India Aparna Lakshmanan S.*, Cochin University of Science and Technology, Kerala, India S. Arumugam, n-CARDMATH, Kalasalingam University, Tamil Nadu, India

Let $f: E \to \{1, 2, 3, ...\}$ be an edge labeling of G. The weight of a path P is the sum of the labels assigned to the edges of P. The edge labeling f is called a geodesic Leech labeling, if the set of weights of the geodesic paths in G is $\{1, 2, 3, ..., t_{gp}(G)\}$, where $t_g p(G)$, the geodesic path number of G, is the number of geodesic paths is G. A graph which admits a geodesic Leech labeling is called a geodesic Leech graph. In this paper, we prove the existence of infinite families of geodesic Leech graphs. It is also proved that C_5 is not a geodesic Leech graph. Some open problems in this area is also included.

Keywords: Leech Labeling, Geodesic path number, Geodesic Leech Labeling, Geodesic Leech Graph