FLORIDA ATLANTIC UNIVERSITY.

Department of Mathematical Sciences Florida Atlantic University

PhD Dissertation Defense

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Lonesum Matrices and Acyclic Orientations:

Enumeration and Asymptotics

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Advisor: Dr. Erik Lundberg

An acyclic orientation of a graph is an assignment of a direction to each edge in a way that does not form any directed cycles. Acyclic orientations of a complete bipartite graph are in bijection with a class of matrices called lonesum matrices, which can be uniquely reconstructed from their row and column sums. We utilize this connection and other properties of lonesum matrices to determine an analytic form of the generating function for the length of the longest path in an acyclic orientation on a complete bipartite graph, and then study the distribution of the length of the longest path when the acyclic orientation is random. We use methods of analytic combinatorics, including analytic combinatorics in several variables (ACSV), to determine asymptotics for lonesum matrices and other related classes.

Please contact Dr. Hongwei Long (hlong@fau.edu) for an electronic copy of the dissertation. ALL ARE CORDIALLY INVITED